Weighted Approximation by Bivariate Generalized Sampling Series

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The present talk deals with weighted approximation of bivariate generalized sampling series. We present pointwise convergence of the series at continuity points of target functions and uniform convergence for weighted uniformly continuous functions. A rate of convergence for the series is also presented via bivariate weighted modulus of continuity and a Voronovskaja theorem for differentiable functions is obtained as well.

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