Runge-Kutta schemes for the numerical solution of linear inhomogeneous IVPs

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Runge-Kutta methods for the numerical solution of inhomogeneous linear initial value problems with constant coefficients [1], [2] is considered.

A general procedure to construct explicit s-stage RK methods with general order s depending on the nodes $c_i, i = 1, ..., s$ is presented. This procedure only requires the solution of successive linear equations in the elements of the matrix **A** and avoids the solution of non linear equations.

Finally, we present several RK schemes with number of stages s = 5, ..., 8 and maximal order p = s for the class of problems under consideration.

References

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