

Numerical methods for 2D linear Fredholm integral equations on curvilinear polygons

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In this talk, we consider the numerical approximation of 2D Fredholm integral equations of the second kind, defined on a curvilinear polygon S (general bi-dimensional domain whose boundary is a piecewise smooth Jordan curve),

$$f(x, y) - \mu \int_S k(x, y, s, t) f(s, t) ds dt = g(x, y), \quad (x, y) \in S,$$

where g and k are given functions defined on S and S^2 , respectively, μ is a fixed real parameter and f is the unknown function in S .

The literature about 2D Fredholm integral equations is not very wide. The methods available mainly consider the case of rectangular domains (see for instance [1] and the references therein). If a global approximation strategy is chosen, the most simple and powerful approach seems to be Nyström methods based on cubature rules obtained as the tensor product of two univariate rules.

On the contrary no global approach was proposed for the case of curvilinear domains that cannot be transformed in a square. On the other hand even if the transformation is possible, the smoothness of the known functions could be not preserved and this can produce a severe loss in the rate of convergence of the method.

Here we propose a numerical method of Nyström type based on cubature formulas introduced in [2]. This choice allows to treat general curvilinear domains, to use a global approximation approach and avoids the loss of convergence due to transformations.

References

- [1] D. Occorsio, M.G. Russo, *Numerical methods for Fredholm integral equations on the square*, Applied Mathematics and Computation 218 (2011), 2318-2333.
- [2] G. Santin, A. Sommariva, M. Vianello, *An algebraic cubature formula on curvilinear polygons*, Applied Mathematics and Computation 217 (2011), no. 24, 10003-10015.