On the improvement of the triangular Shepard method by non conformal elements

F. Dell'Accio^{*a*}, F. Di Tommaso^{*a*}, A. Guessab^{*b*}, F. Nudo^{*a*}

^a Dipartimento di Matematica e Informatica, Università della Calabria, (Italy)
^b Laboratoire de Mathématiques et de leurs Applications, UMR CNRS 4152, Université de Pau et des Pays de l'Adour, (France)
francesco.dellaccio@unical.it, filomena.ditommaso@unical.it, allal.guessab@univ-pau.fr, federico.nudo@unical.it

Most classical numerical methods for approximation of a multivariate function (or integrals of it) use function values at sample points. However, as shown in [2, 3], in many practical problems, the available data are not restricted by function evaluations, but contain several integrals over certain hyperplane sections, or, more generally, over smooth surfaces in \mathbb{R}^d . In such cases, generalizations of the existing theory and algorithms of approximation operators are required, which are based on the enriched set of data. In this work, we focus on this problem in the two dimensional case, in the setting of scattered data. More precisely we construct new Shepard type approximation operators, based on new enrichments of the standard linear triangular element, using polynomial functions. In line with previously considered improvements of the triangular Shepard method [4, 5], these enriched triangular elements will be blended by using triangular Shepard basis functions [1]. Numerical results are provided.

References

- F. Dell'Accio, F. Di Tommaso, K. Hormann, On the approximation order of triangular Shepard interpolation, IMA Journal of Numerical Analysis, Volume 36 (2016), pp. 359–379.
- [2] A. Guessab, B. Semisalov, A multivariate version of Hammer's inequality and its consequences in numerical integration, Results in Mathematics, Volume 73 (2018), pp. 1–32.
- [3] A. Guessab, B. Semisalov, Numerical integration using integrals over hyperplane sections of simplices in a triangulation of a polytope, Bit Numerical Mathematics, Volume 58 (2018), pp. 1–48.
- [4] F. Dell'Accio, F. Di Tommaso, O. Nouisser, B. Zerroudi, *Increasing the approximation order of the triangular Shepard method*, Applied Numerical Mathematics, Volume 126 (2018), pp. 78–91.
- [5] F. Dell'Accio, F. Di Tommaso, O. Nouisser, B. Zerroudi, Fast and accurate scattered Hermite interpolation by triangular Shepard operators, Journal of Computational and Applied Mathematics, Volume 382 (2021), pp. 113092.